

COMBINED SPLINES IN SMOOTHING HISTOPOLATION

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Our talk deals with space $S(T, A_1 \times A_2)$ of combined splines [1] defined by continuous linear operators $A_1 : X \rightarrow \mathbb{R}^n$, $A_2 : X \rightarrow \mathbb{R}^m$ and $T : X \rightarrow Y$ in Hilbert spaces X and Y . Such splines give us a possibility to take into account interpolation conditions of two different types described by A_1 and A_2 correspondingly.

For given vectors $\mathbf{u} \in \mathbb{R}^n, \mathbf{v} \in \mathbb{R}^m$ and parameters $\delta, \omega, \varepsilon_i > 0$, $i = 1, \dots, n$, we consider the following conditional minimization problems:

$$\|Tx\|^2 + \frac{1}{\omega} \|A_1x - \mathbf{u}\|^2 \longrightarrow \min_{A_2x = \mathbf{v}}, \quad \|Tx\| \longrightarrow \min_{\|A_1x - \mathbf{u}\| \leq \delta, A_2x = \mathbf{v}},$$

$$\|Tx\| \longrightarrow \min_{|(A_1x)_i - u_i| \leq \varepsilon_i, i = 1, \dots, n, A_2x = \mathbf{v}}.$$

The aim of this talk is to present some results on solutions of these problems obtained under the assumptions:

$\text{Ker}T \cap \text{Ker}A_1 \cap \text{Ker}A_2 = \{0\}$, $A_1(X) = \mathbb{R}^n$, $A_2(X) = \mathbb{R}^m$, $T(\text{Ker}A_1 \cap \text{Ker}A_2)$ is closed.

In particular we consider the problem of approximation of a given histogram with boundary conditions by taking

$$Tx = x^{(r)}, \quad (A_1x)_i = \int_{t_{i-1}}^{t_i} x(t)dt, \quad i = 1, \dots, n, \quad (A_2x)_1 = x(a), \quad (A_2x)_2 = x(b), \quad x \in W_2^r[a, b].$$

This investigation is closely related to our previous works on smoothing histopolation [2], [3].

REFERENCES

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